## Mathematics B T065

Wednesday, 30/10/2013 8: 30-11: 30 AM

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## ADVANCED LEVEL NATIONAL EXAMINATION, 2013, TECHNICAL AND PROFESSIONAL TRADES

## EXAM TITLE: Mathematics B

## OPTIONS:

| 01. Electricity | (ELC) | 07. Computer Electronics | (CEL) |
| :--- | :--- | :--- | ---: |
| 02. Graphic Arts | (ART) | 08. Electronics and |  |
| 03. Sculpture Ceramics | (SCE) | Telecommunication | (ETL) |
| 04. Carpentry | (CAP) | 09. General Mechanics | (GME) |
| 05. Tailoring | (TAL) | 10. Motor Vehicle Mechanics (MVM) |  |
| 06. Construction | (CST) | 11. Public Works | (PWO) |

## DURATION: 3hours

## INSTRUCTIONS:

The paper contains two (2) Sections:
Section I: Fifteen (15) Compulsory Questions 55marks
Section II: Five (5) questions, choose three (3) 45marks

## Section I: Attempt all 15 questions. 55marks

1. Find the values of x which satisfy the equation $2 x^{2}-3 x=0$.

2marks
02. Solve in $I R$ the equation $\sqrt{x+6}+x=14$.

3marks
03. Given that $f(x)=3-7 x+5 x^{2}-x^{3}$, show that $3-x$ is a factor of $f(x)$. Factorize $f(x)$ completely and hence state the set of values for which $f(x) \leq 0$.

4marks
04. Solve, using substitution, the following simultaneous equations.

3marks

$$
\left\{\begin{array}{c}
y+7=12 x-3 x^{2} \\
13=9 x-y
\end{array}\right.
$$

5. For what value of d does $p(x)=x^{2}+d x+4$ yield the same remainder when divided by either $x-1$ or $x-3$ ?
6. Find centre and radius of the circle represented by the following equation : $x^{2}+y^{2}-4 x+2 y-11=0$.
7. Find the coordinates of the points where the curve
$y=x^{3}+6 x^{2}+11 x+6$ cuts :
(a) The $y$-axis.

4marks
(b) The $x$-axis.
08. Evaluate: $\lim _{x \rightarrow 1} \frac{\sqrt{5 x-4}-\sqrt{x}}{x-1}$.
09. Find all the angles between 0 and $2 \pi$ which satisfy the equation

$$
(1+2 \sin x) \cos 2 x=0
$$

4marks
10. Find the point where the line joining $(3,2,1)$ and $(5,4,2)$ cuts the plan $x+y+2 z=19$.

4marks
11. The sum of the first and fourth terms of an arithmetic sequence is 2 , and the sum of their squares is 20.
i. Find the common difference
ii. Find the sum of the first eight terms of the sequence.
12. If $V=30 t-6 t^{2}$, find $\frac{d V}{d t}$ and hence find the maximum value of V and the value of $t$ for which it occurs.

3marks
13. Find the equations of asymptotes of the following function:

$$
y=\frac{x^{2}+5 x+4}{x}
$$

## 4marks

14. Given that $z_{1}=3+2 i$ and $z_{2}=4-3 i$,
i. Find $z_{1} z_{2}$ and $\frac{z_{1}}{z_{2}}$, each in the form $a+b i$.
ii. Verify that $\left|z_{1} z_{2}\right|=\left|z_{1}\right|\left|z_{2}\right|$.

5marks
15. Evaluate $\int_{3}^{4} \frac{3}{x^{2}-4} d x$, correct to 3 significant figures.

5marks

## Section II: Attempt any three (3) questions 45marks

16. Given the function $f(x)=\frac{1}{x-3}+2$.
a) Find the domain of definition.

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b) Find asymptotes to the curve.

3marks
c) Compute the first derivative and study its sign.
d) Compute the second derivative and study its sign.

3marks
e) Find the variation table.

2marks
f) Find intercept point with axes.

2marks
g) Sketch the graph of function $f(x)$.
17. The table below shows marks scored by 10 students in physics and mathematics
tests.

(a) Represent the data above on a scatter diagram.
(b) Find means, variances, covariance and standard deviations

## 2marks

6marks
(c) Find an equation of line of best fit (regression line) in the form:

$$
y=a+b x
$$

3marks
(d) If a student scored 7.5 in physics, predict his score in mathematics.
(e) Find coefficient of correlation.


2marks

2marks
18. a) Given a complex number $z=\left(\frac{-1}{2}+i \frac{\sqrt{3}}{2}\right)$
i. Put $z$ in polar form (trigonometric form)

3marks
ii. Calculate $z^{2014}$; leave your answer in algebraic form $(a+b i)$. 3marks
iii. Find the fourth roots of $z$. Leave your answer in algebraic form $(a+b i)$.

5marks
b) In argand diagram, the point $P$ represents the complex number.

Given that $|z-1-i|=\sqrt{2}$, Sketch the locus of $P$.
4marks
19. a) The curves $y=2 x^{2}-3 x$ and $y=x^{2}$ intersect at two points.
i. Find these points of intersection.

3marks
ii. Find the equation of the straight line joining these points.

3marks
b) Given a triangle with vertices $A(1,-2,3) ; B(2,4,-1)$ and $C(1,3,2)$.
i. Find equations of sides.
ii. Find equation of the plane ABC .

3marks
iii. Find area of the triangle $A B C$.
20. a) Solve the following equations:
i. $6^{3 x+1}=7^{2-x}$.

3marks
ii. $\left\{\begin{aligned} 5 x+4 y & =12 \\ \ln (x-1)+\ln y & =\ln 3-\ln 5\end{aligned}\right.$

3marks
iii. $e^{2 x}+3 e^{x}-4 \doteq 0$

3marks
b) Evaluate the following integrals
i. $\int_{0}^{\pi / 2}(5 \sin 3 x+2 \cos x) d x$

3marks
ii. $\int_{0}^{1}\left(\frac{x}{x+1}\right) d x$

